



# Jet Noise Modeling and Prediction using Steady RANS Solutions

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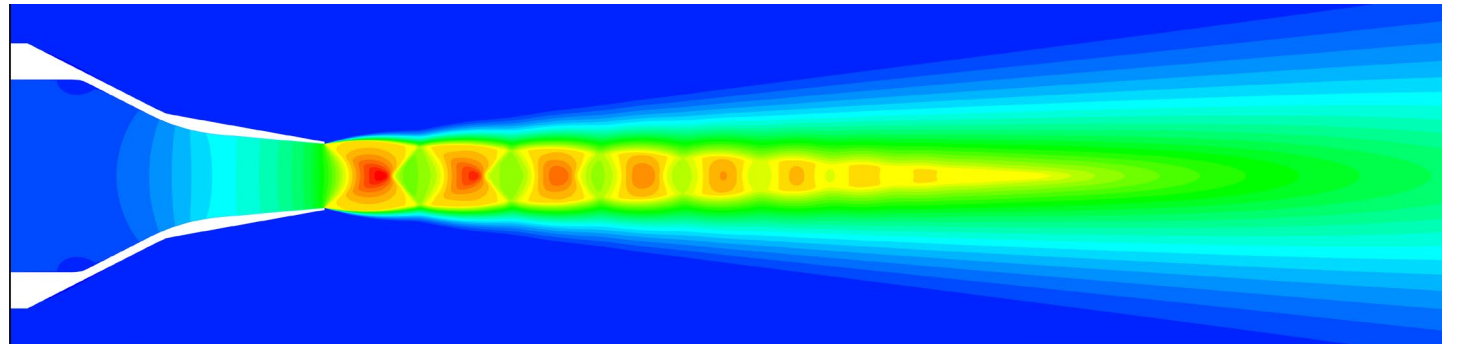
Ing. Francesco Petrosino



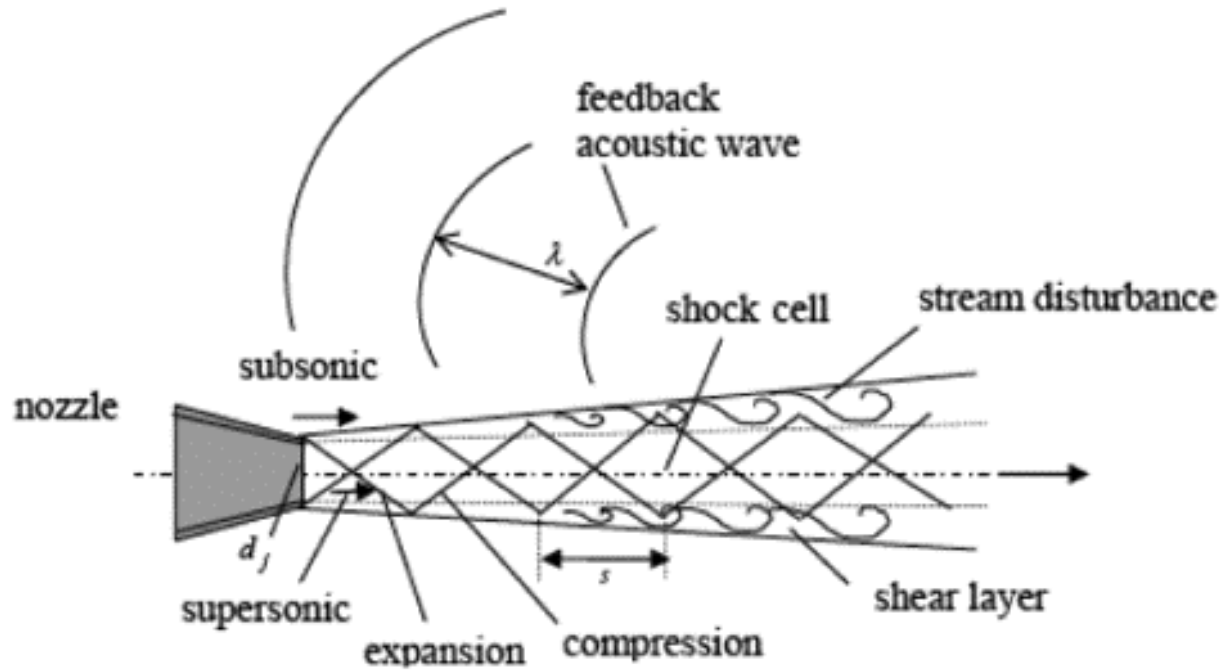
# Target



Implement a computational procedure to evaluate the noise disturbance caused by aircraft's jets using high order models



# Jet Noise Description



## Mixing Noise

Large-Scale Coherent Noise

Fine-Scale Incoherent Noise

## Shock Associated Noise

Broad-Band Shock-Associated Noise

Screech

# Acoustic Analogy Model

## Model Features

- Acoustic analogy model based on the linearized Euler equations (LEE)
- Ability to separate source terms from propagation terms
- Full compatibility with both components of 'noise' considered
  - Mixing noise
  - BBSAN

## Working Assumptions

- Observer far from the jet
- Absence of a mean flow field
- Proudman hypothesis for isotropic turbulence

## Model governing equations

$$\frac{\partial \pi'}{\partial t} + \bar{u}_j \frac{\partial \pi'}{\partial x_j} + \frac{\partial u'_i}{\partial x_i} = \theta$$

$$\frac{\partial u'_i}{\partial t} + \bar{u}_j \frac{\partial u'_i}{\partial x_j} + u'_j \frac{\partial \bar{u}_i}{\partial x_j} + \bar{a}^2 \frac{\partial \pi'}{\partial x_i} = f_i$$

# Acoustic Analogy Model: Final Equations

## Mixing Noise

$$S(\mathbf{x}, \omega) = \rho_\infty^2 a_\infty^4 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{2\pi^{3/2} a_\infty^2 l_x l_y l_z x^2 \tau_s}{a_\infty^2 x^2 + (a_\infty x + \bar{u}x_1 + \bar{v}x_2 + \bar{w}x_3)^2 \tau_s^2 \omega^2} \left\{ \left[ \pi_g^{*0}(\mathbf{x}, \mathbf{y}, \omega) \pi_g^0(\mathbf{x}, \mathbf{y}, \omega) A_s^2 \frac{(u_s/a_\infty)^4}{\tau_s^2} \right] + \right. \\ \left. + \sum_{n=1}^3 \sum_{m=1}^3 \pi_g^{*n}(\mathbf{x}, \mathbf{y}, \omega) \pi_g^m(\mathbf{x}, \mathbf{y}, \omega) B_s^2 \frac{(u_s/a_\infty)^2 u_s^2}{l_x^2} \right\} \exp \left[ -\frac{\omega^2 (l_x^2 x_1^2 + l_y^2 x_2^2 + l_z^2 x_3^2)}{4a_\infty^2 x^2} \right] d\mathbf{y}$$

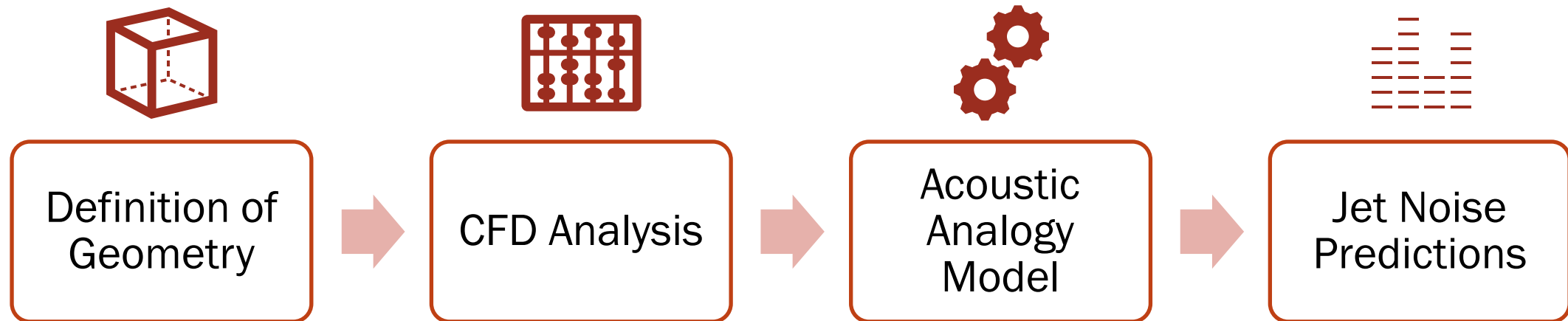
## Broad-Band Shock-Associated Noise

$$S(\mathbf{x}, \omega) = \pi^{1/2} \rho_\infty^2 a_\infty^4 \int_{-\infty}^{\infty} \cdots \int_{-\infty}^{\infty} \left\{ \sum_{n=1}^3 \sum_{m=1}^3 \pi_g^{*n}(\mathbf{x}, \mathbf{y}, \omega) \pi_g^m(\mathbf{x}, \mathbf{y}, \omega) \frac{x^2}{x_n x_m} \frac{2K(\mathbf{y}) l_y l_z \tau_s}{3\bar{\rho}^2 \bar{u}^2 l_x} p_s(\mathbf{y}) \tilde{p}_s(k_1, y_2, y_3) \right\} \times \\ \times \frac{1}{\left[ 1 + \left( 1 - \frac{\bar{u}}{a_\infty} \cos \theta + \frac{\bar{u} k_1}{\omega} \right)^2 \omega^2 \tau_s^2 \right]} \exp \left[ -\frac{l_x^2}{4} \left( \frac{\omega}{a_\infty} \cos \theta - k_1 \right)^2 - \frac{\omega^2 l_y l_z}{4a_\infty^2} \sin^2 \theta \right] dk_1 d\mathbf{y}$$

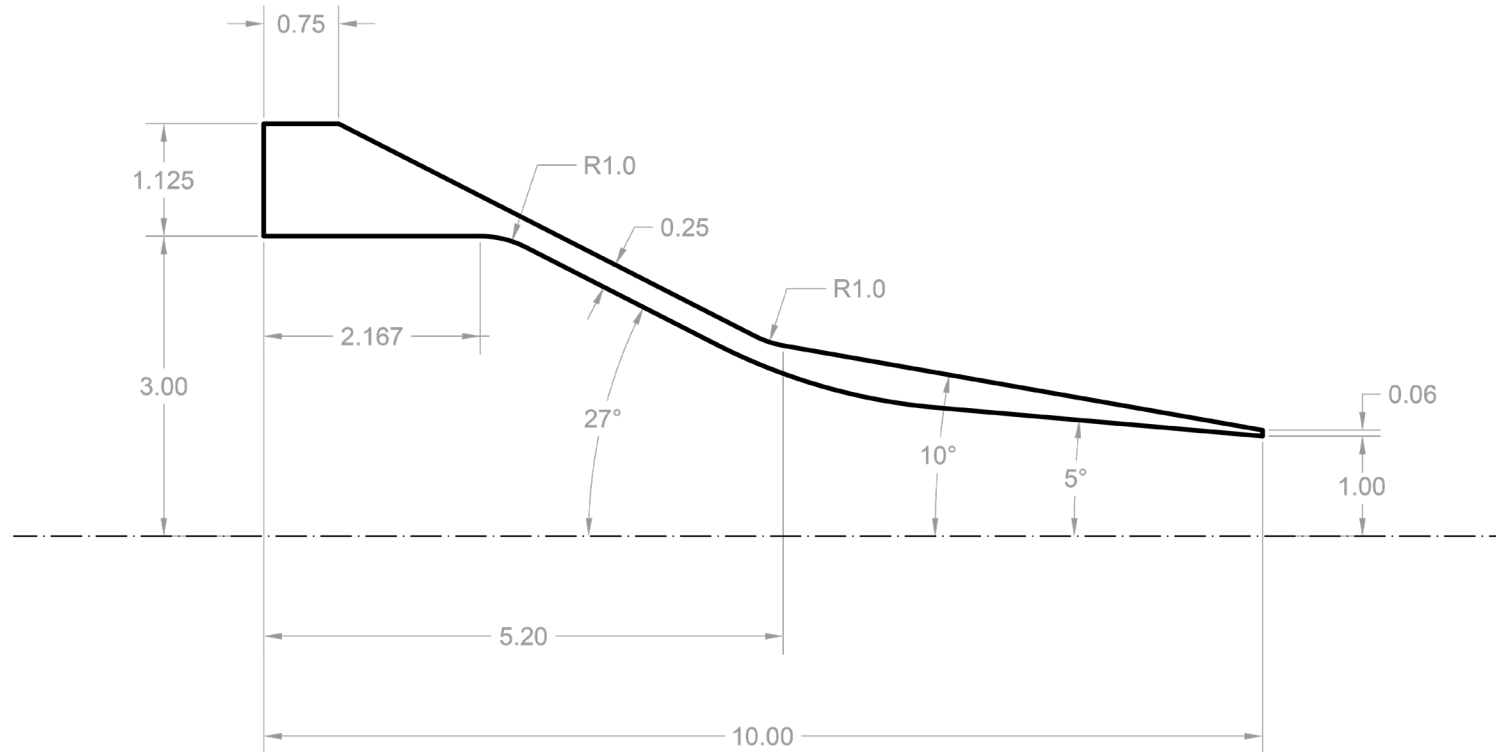
## Green's Function

$$\pi_g^n(\mathbf{x}, \mathbf{y}, \omega) = \frac{i\omega x_n}{4\pi a_\infty^3 x^2} \exp \left[ \frac{-i\omega x}{a_\infty} \right] \delta_{in} + \frac{i\omega}{4\pi a_\infty^2 x} \exp \left[ \frac{-i\omega x}{a_\infty} \right] \delta_{0n}$$

# Overview of the Process



# Definition of Geometry: SMC000 Nozzle



## Geometric Dimensions

- Axial Symmetry
- $L = 0.254 \text{ m}$
- $D_1 = 0.1524 \text{ m}$
- $D_2 = 0.0508 \text{ m}$
- $\frac{A_1}{A_2} = 9$

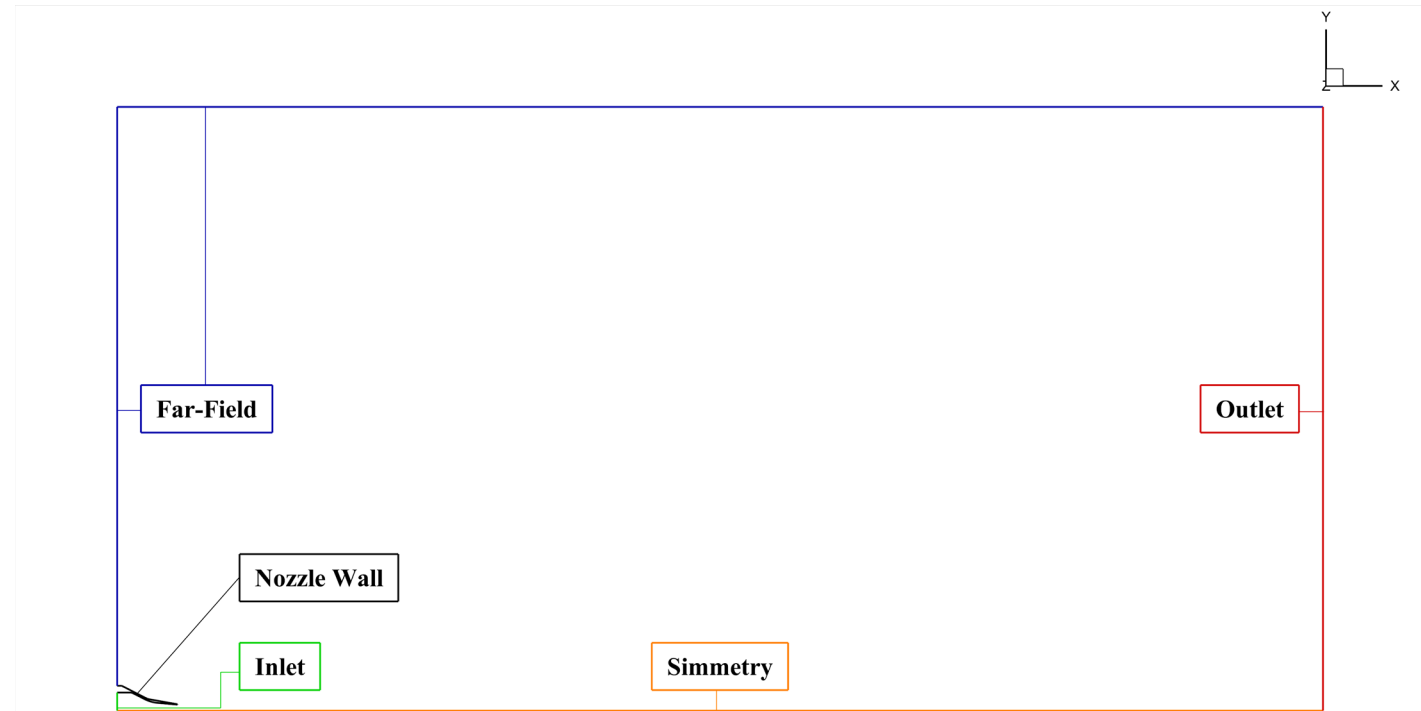
# Definition of the Computational Domain

## Dimensions:

- $L_x = 100 \cdot D_2$
- $L_y = 50 \cdot D_2$

## Boundary Conditions:

- Inlet
- Far-Field
- Axis of symmetry
- Nozzle Walls
- Outlet





# Test Case and Computational Grid

## Type of Simulation

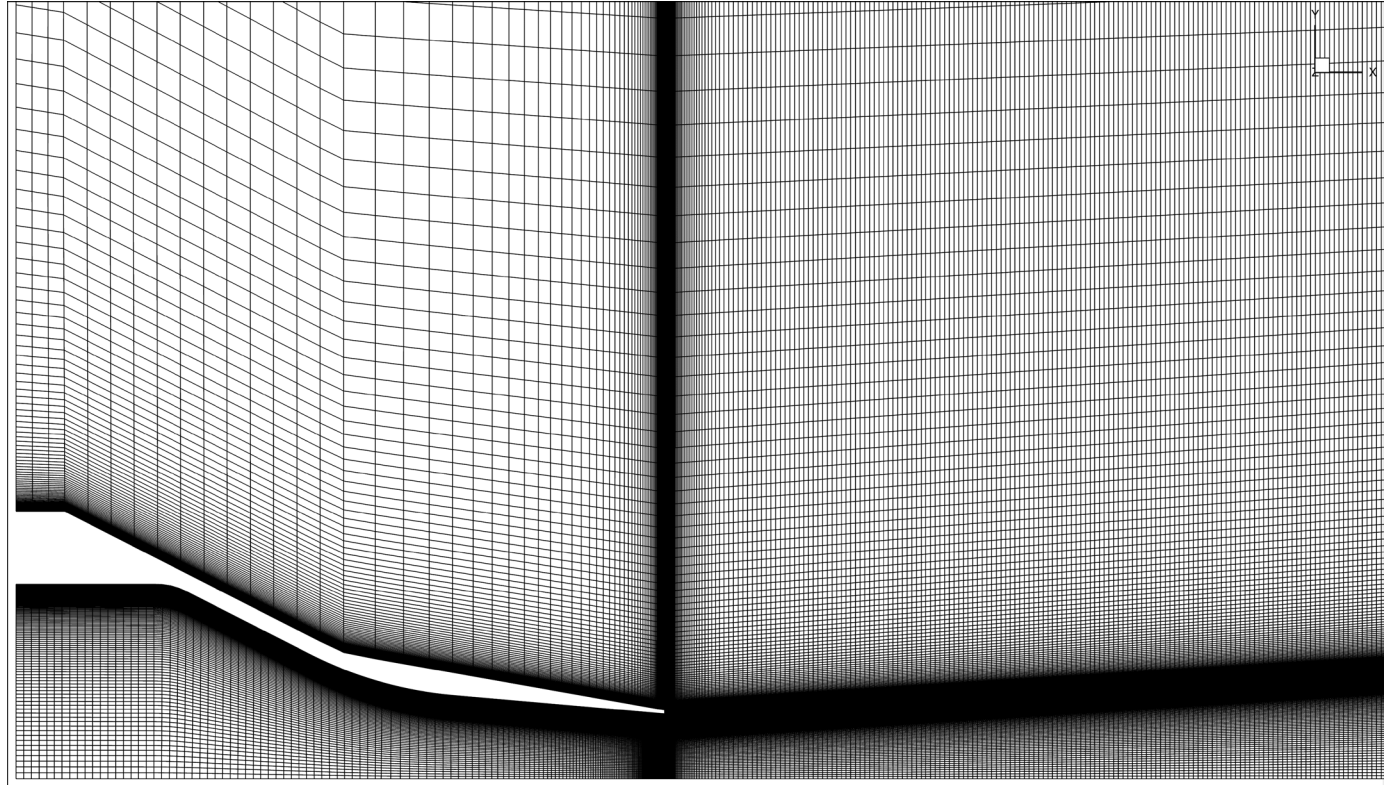
- Steady RANS with  $k - \omega$  SST closure model

## Operating Conditions

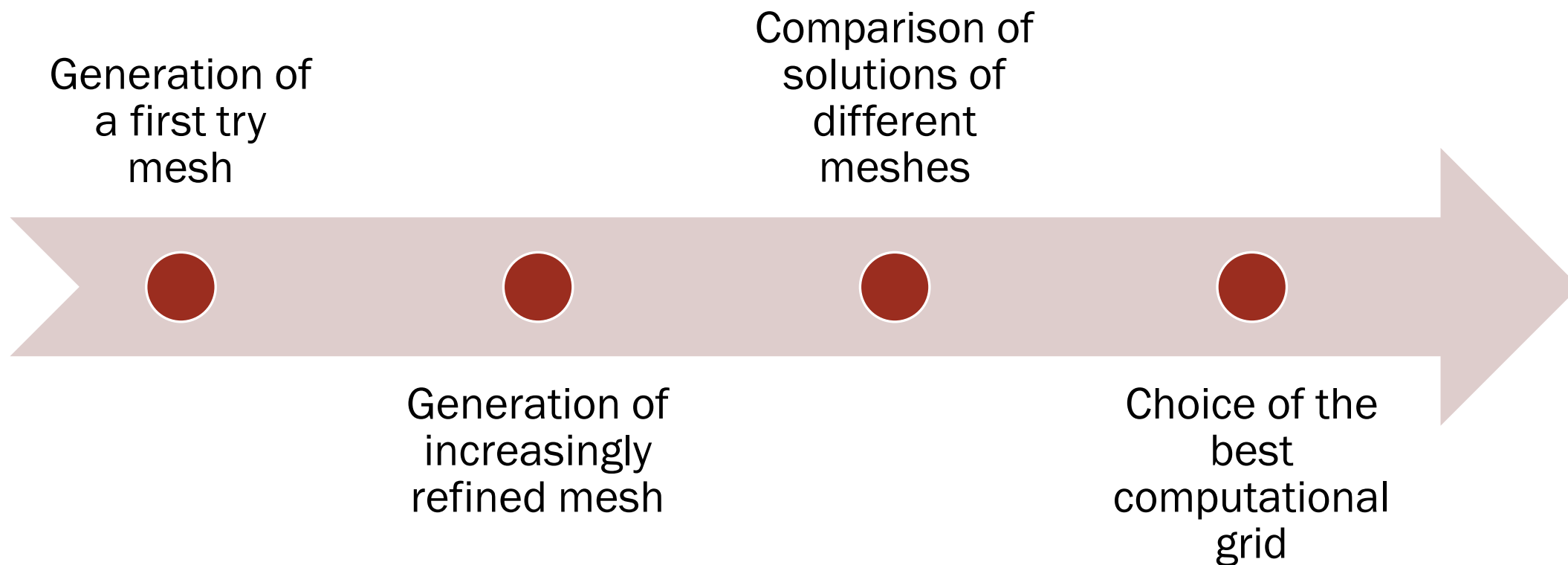
- $M_j = 1.47$
- $M_d = 1.00$
- $TTR = 1.00$

## Free-stream Conditions

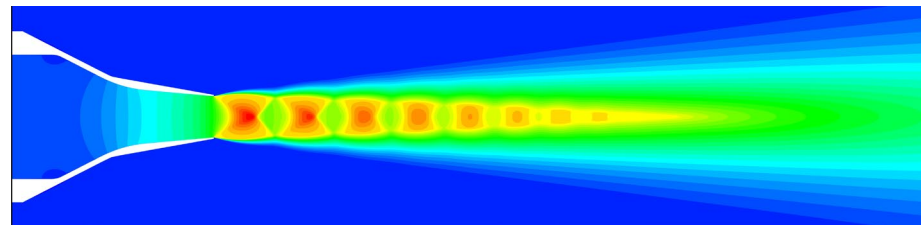
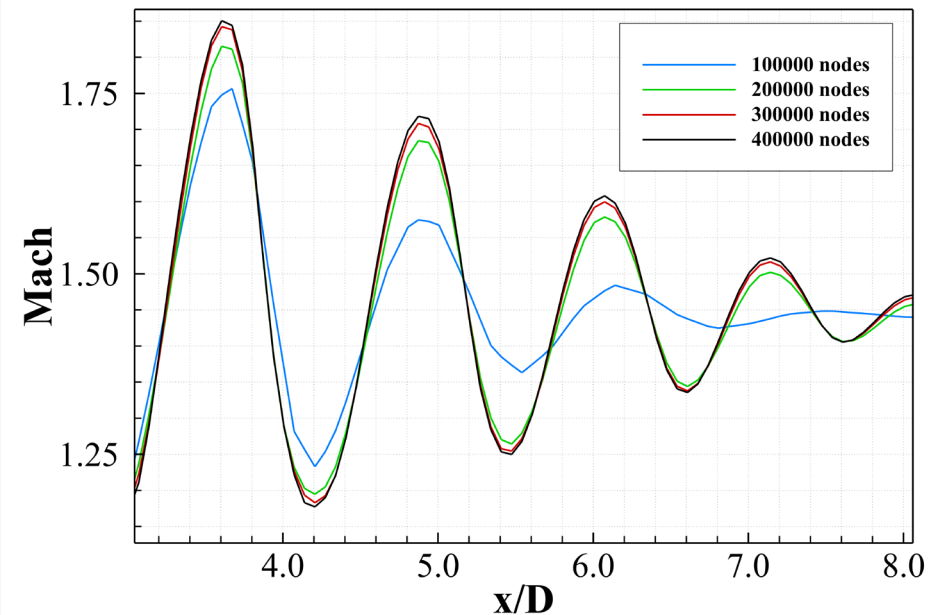
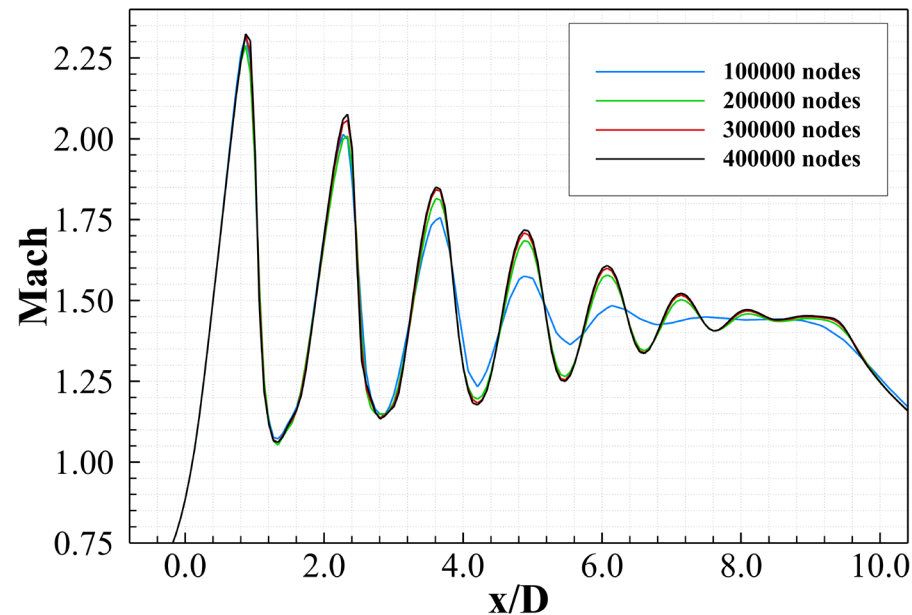
- $p_\infty = 101325 \text{ Pa}$
- $T_\infty = 293.15 \text{ K}$



# Grid Convergence Study



# Grid Convergence Study



# CFD Solution Validation

Reference solution performed with

FUN3D

- Turbulence closure model:  $k - \omega$  SST
- With compressibility correction

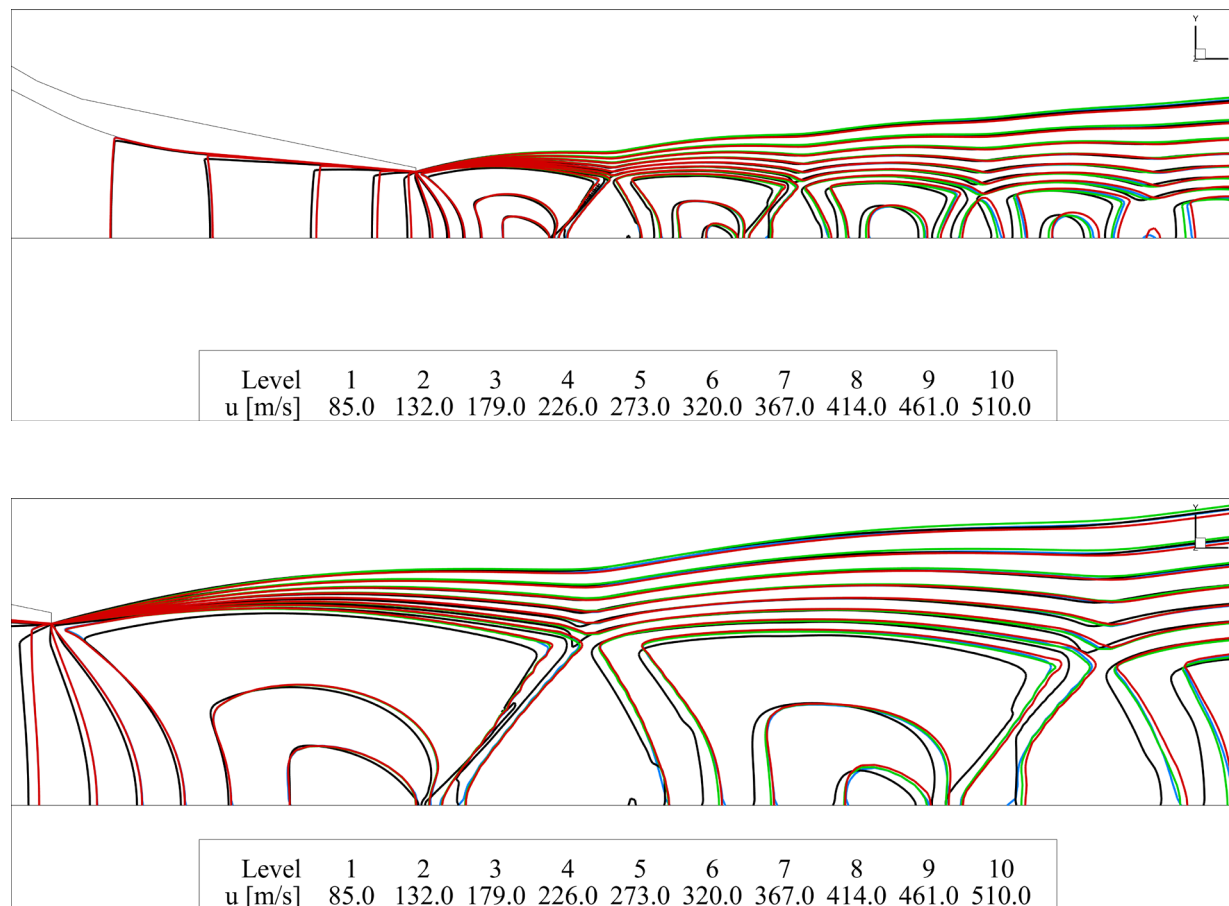
CFD simulations performed with

Ansys Fluent

- Turbulence closure model:  $k - \omega$  SST
- With compressibility correction
- Without compressibility correction

SU2

- Turbulence closure model:  $k - \omega$  SST
- Without compressibility correction

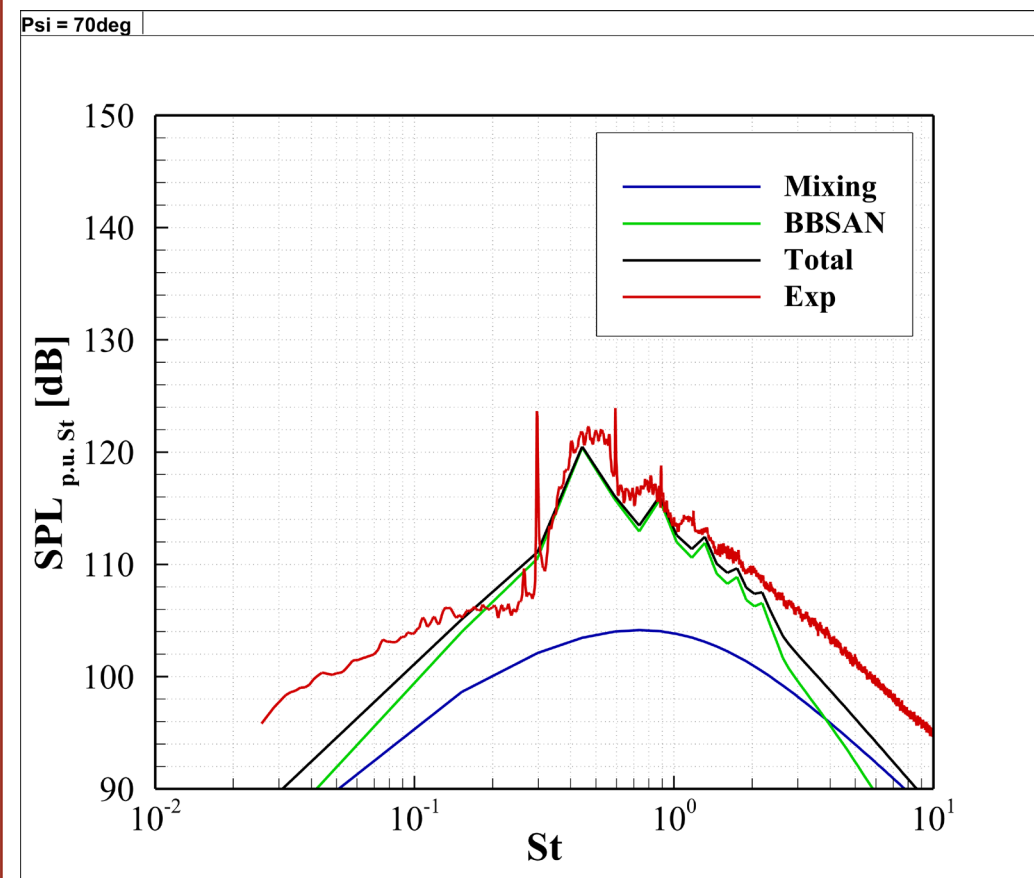
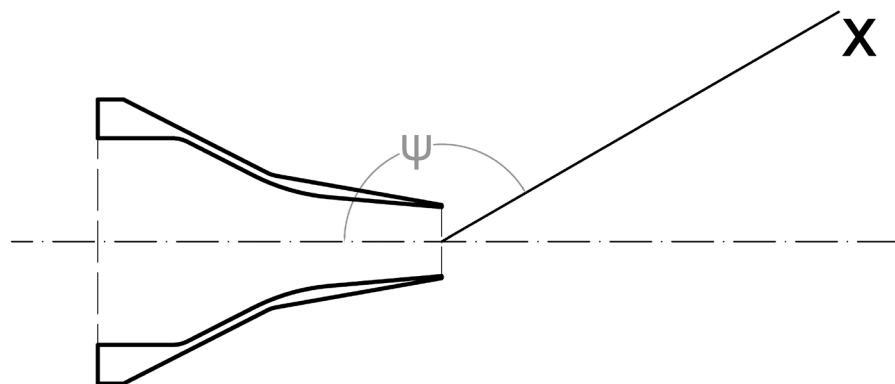




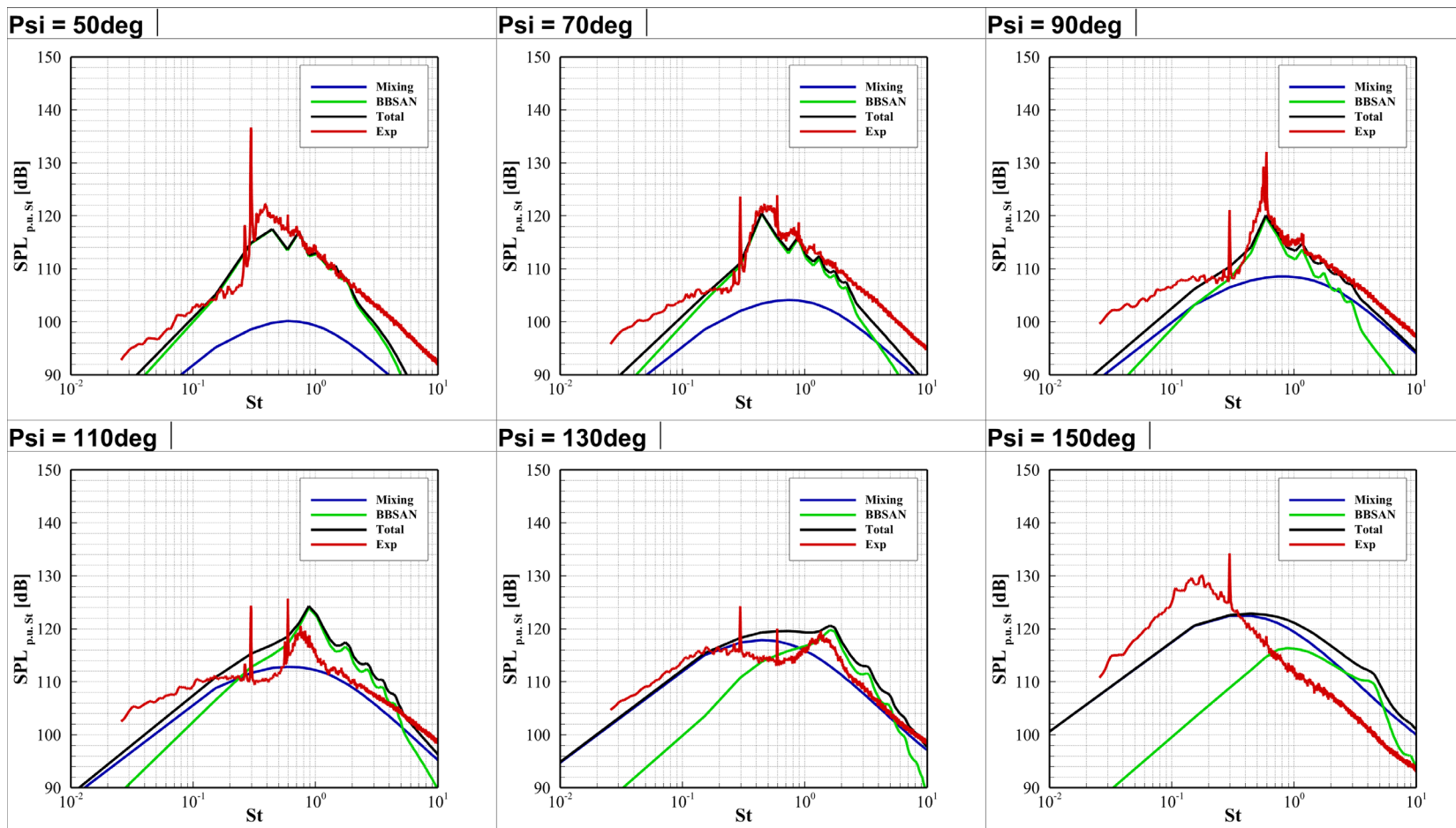
# Results: Test case SMC0003

## Operating Conditions

$$M_j = 1.47; \quad M_d = 1.00; \quad TTR = 1.00$$



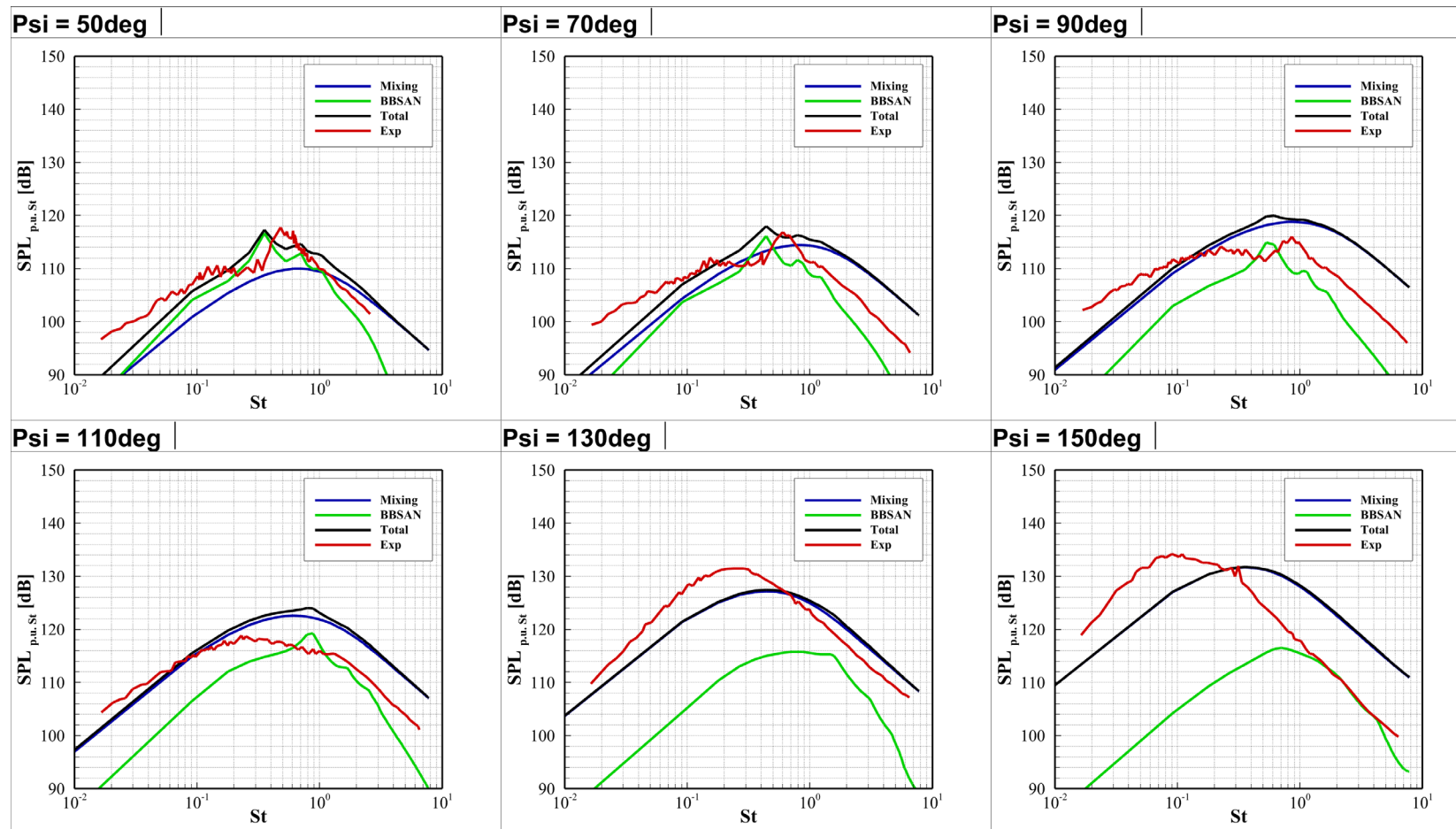
# Results: Test case SMC0003



# Results: Test case SMC0008

## Operating Conditions

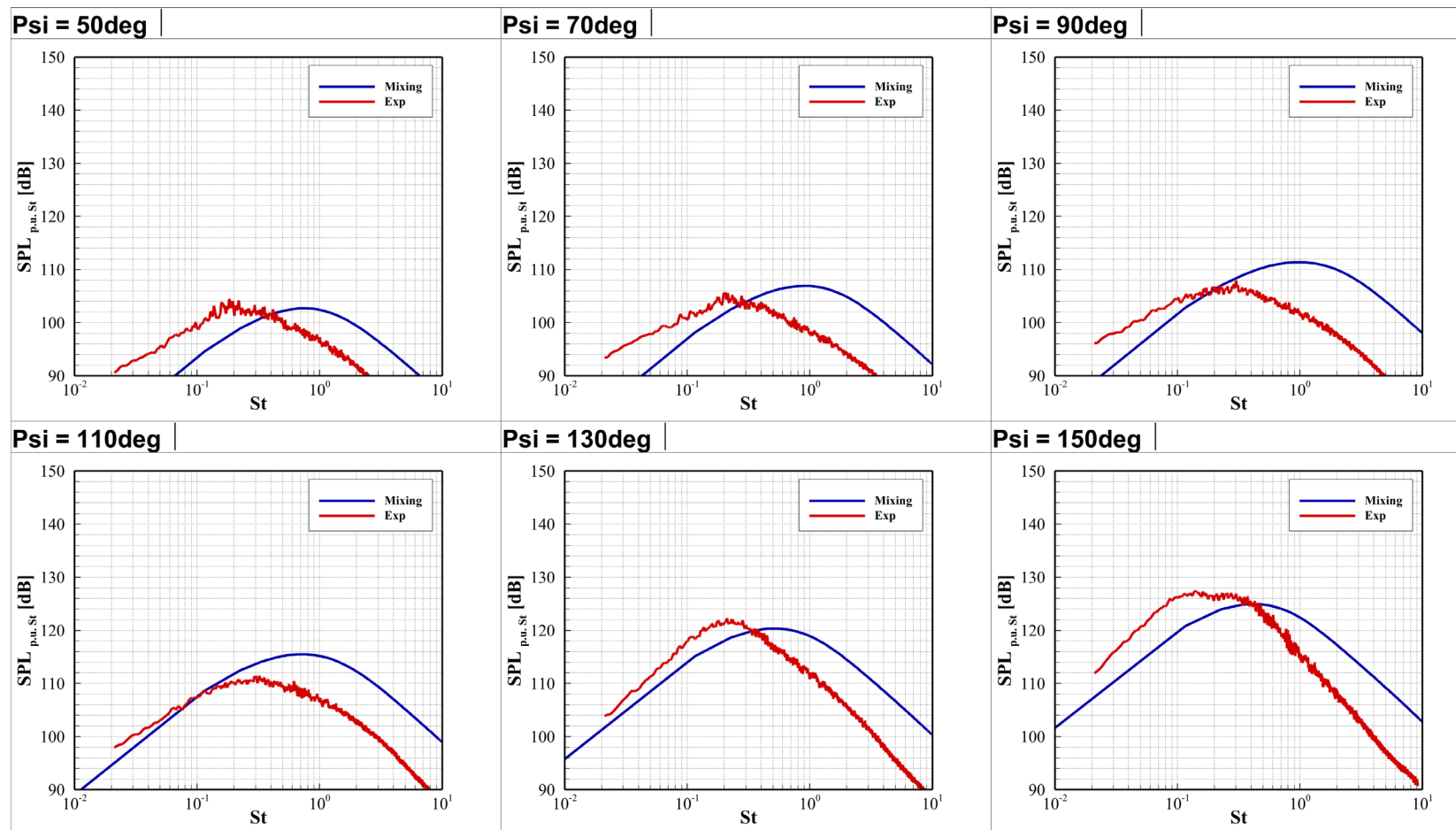
- $M_j = 1.24$
- $M_d = 1.00$
- $TTR = 3.20$



# Results: Test case SMC0004

## Operating Conditions

- $M_j = 1.00$
- $M_d = 1.00$
- $TTR = 2.70$





# Conclusions



- Study of different aeroacoustics models
- Implementation of the acoustic model based on LEE
- Calculation of CFD solutions to be provided to the acoustic solver
- Comparison of the fluid dynamics solution with reference data
- Validation of the acoustic solver on experimental test cases

# Future Developments



- Develop a solver for calculating more complex Green's functions of linearized Euler equations
- Test different closure models for the turbulence equations
- Test different compressibility correction models related to the turbulence closure equations
- Integrate into the solver different source models
- Optimize the acoustic solver to improve computation time
- Use this tool to optimize nozzle geometry

# Reference Acoustic Models

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- Morris and Farassat. Acoustic analogy and alternative theories for jet noise prediction. 2002.
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- Miller. Towards a comprehensive model of jet noise using an acoustic analogy and steady RANS solutions. 2014.

# Thank you for your attention